

6-5 Factoring $ax^2 + bx + c$

Things to remember:

Start

End

$$ax^2 + bx + c$$

$$(_x + _)(_x + _)$$

$$ax^2 - bx + c$$

$$(_x - _)(_x - _)$$

$$ax^2 + bx - c$$

$$(_x + _)(_x - _)$$

$$ax^2 - bx - c$$

$$(_x + _)(_x - _)$$

Steps:

- 1.) Factor out GCF if possible
- 2.) Find the factors of a and put those values in the 1st blanks.
- 3.) Find the factors of c and put those values in the last blanks.
- 4.) Multiply the outside and inside and add to get b.
- 5.) If you don't get b, try again.

Factor.

$$a=21 \quad b=13 \quad c=2$$
$$21x^2 + 13x + 2$$

$$a=8 \quad b=14 \quad c=3$$
$$8x^2 + 14x + 3$$

No. $\frac{(3x+2)(7x+1)}{N} \quad N \frac{(2x+1)(4x+3)}{O}$

$3x+14x=17x$

$(3x+1)(7x+2)$

$6x+7x=13x$

$6x+4x=10x$

$(4x+1)(2x+3)$

$12x+2x=14x$

Factor.

$$a=18 \quad b=36 \quad c=14$$

$$\frac{18x^2 + 36x - 14}{2} \quad \text{GCF: 2}$$

$$a=9 \quad b=18 \quad c=7$$

$$2(9x^2 + 18x - 7)$$

$$\boxed{2(3x+7)(3x-1)}$$

$$-3x + 2 | x = 18x$$

$$\begin{array}{r} 9 \\ 18 \\ \hline 3 \times 3 \end{array} \quad \begin{array}{r} 7 \\ 14 \\ \hline 1 \times 7 \end{array}$$

Factor.

$$a=4 \quad b=2 \quad c=6$$

$$\frac{4a^2 + 2a - 6}{2} \quad GCF: 2$$

$$2(2a^2 + 1a - 3) \quad \begin{matrix} a=2 \\ b=1 \\ c=-3 \end{matrix}$$

$$2(2a+3)(2a-1)$$

$$\cancel{2(2a+3)(2a-1)}$$

$$-1a+6a=5a$$

$$2(2a+3)(1a-1)$$

$$-2a+3a=1a$$

$$a=8 \quad b=0 \quad c=2$$

$$\frac{8x^2 - 2}{2} \quad GCF: 2$$

$$2(4x^2 - 1)$$

$$2(2x+1)(2x-1)$$

$$\cancel{2(4x^2 + 0x - 2)} \quad GCF: 2$$

$$2(4x^2 + 0x - 1) \quad a=4 \quad b=0 \quad c=-1$$

$$2(-x+1)(3x-1)$$

Factor

$$6x^2 - 41x - 7$$

$$a=6 \quad b=-41 \quad c=-7$$

$$(3x+1)(2x-7)$$

$$-3x + 14x = 11x$$

$$(3x+1)(2x-7)$$

$$-21x + 2x = -19x$$

$$6m^2 + 15mn - 9n^2$$

$$(-m-3)(-m+3)$$

$$(6x+1)(1x-7)$$

$$-42x + 1x = -41x$$